# Contest Corner: The 2016 State Tournament of Mathematics Results 

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#### Abstract

In this article, the authors summarize results from the 2016 Ohio Mathematics Tournament. Included in the summary are sample tasks from the contest.


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## 1 Introduction

This year the State Tournament of Mathematics found Ohio experiencing very mild weather with average temperatures near 50 degrees across the state. Inclement weather that has affected the tournament in previous years was a non-factor. The 43rd State Tournament of Mathematics took place on February 27th and now is the time to start assembling a team to represent your school in the 2017 competition. The 2017 tournament will take place on March 4, 2017, at test centers located throughout Ohio. You can find registration information on the OCTM State Tournament of Mathematics at www. octmtournament. org. A total of 1107 students representing 80 schools competed this year. The overall results for the top 22 schools are summarized in Table 1.

Table 1: 2016 Overall State Tournament Results

| Rank | School | Score | Rank | School | Score |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | William Mason High School | 152 | 12 | Revere High School | 118 |
| 2 | Dublin Jerome High School | 146 | 13 | Hudson High School | 116 |
| 3 | Columbus Academy High School | 143 | 13 | Summit Country Day School | 116 |
| 4 | Sycamore High School | 139 | 13 | Upper Arlington High School | 116 |
| 5 | Dublin Coffman High School | 133 | 16 | Brecksville-Broadview Heights | 114 |
| 6 | Copley High School | 131 | 16 | Walnut Hills High School | 114 |
| 7 | Western Reserve Academy School | 128 | 18 | Hilliard Darby High School | 113 |
| 8 | Seven Hills Upper School | 120 | 19 | Lakota West High School | 106 |
| 8 | Thomas Worthington High School | 120 | 19 | St. Vincent-St Mary High School | 106 |
| 8 | Westlake High School | 120 | 19 | St. Xavier High School | 106 |
| 11 | Avon Lake High School | 119 |  |  |  |

As has been done for many years, the OCTM also presented awards and recognition to participating schools by their size. In this way, small schools are not put in direct competition with larger schools. OCTM uses a five level system to group schools. For 2016 Level 1 schools have fewer than 95 students per grade level, Level 2 schools have from 95 and 171 students per grade level, Level 3 schools have from 172 and 286 students per grade level, Level 4 schools have from 287 and 406 students per grade level and Level 5 schools have more than 406 students per grade level. Tables 2 and 3 show the 2016 tournament results by level.

Table 2: 2016 State Tournament Results by Level (Levels 1-3)

| Level 1: $(n \leq 94)$ | Level 2: $(94<n \leq 171)$ | Level 3: $(171<n \leq 286)$ |
| :---: | :---: | :---: |
| 1143 Columbus | 1128 Western Reserve | 1131 Copley |
| 2120 Seven Hills Upper | 2106 St Vincent-St Mary | 2118 Revere |
| 3116 Summit Country Day | 3103 Beachwood | 3103 Aurora |
| 492 Wellington | 3103 Hathaway Brown | 497 Archbishop Hoban |
| 580 Ayersville | 596 Hawken Upper | 595 Lake |
| 679 Dayton Christian HS | 694 Cincinnati Hills Christian | 595 Rocky River |
| 679 Trinity | 791 Gilmour | 792 Shawnee |
| 876 Cincinnati Country Day | 876 Edison | 885 Poland Seminary |
| 972 Worthington Christian | 975 Carlisle | 980 Ashland |
| 1071 Bluffton | 1072 Jonathan Alder | 980 Celina |
| 1071 Kirtland | 1168 Bio-Med Science | 1179 Carroll |
| 1071 Miami Valley | 1260 Black River | 1274 Ross |
| 1355 Highland | 1362 Central Catholic | 1373 Perkins |
| 1435 Columbus N Intern | 1459 Lake Ridge | 1457 Walsh Jesuit |
| 1535 Shelby | 1541 Purcell Marian | 1547 Madison |

Table 3: 2016 State Tournament Results by Level (Levels 4-5)

| Level 4: $(286<n \leq 406)$ | Level 5: $(406<n)$ |
| :--- | :--- |
| 1 146 Dublin Jerome | 1152 William Mason |
| 2139 Sycamore | 2133 Dublin Coffman |
| 3120 Westlake | 3120 Thomas Worthington |
| 4119 Avon Lake | 4116 Upper Arlington |
| 5 116 Hudson | 5114 Walnut Hills |
| 6 114 Brecksville-Broadview Hts | 6106 Lakota West |
| 7 113 Hilliard Darby | 7103 Strongsville |
| 8 106 St Xavier | 897 Jackson |
| 9 98 Perrysburg | 994 Berea-Midpark |
| 10 96 Mayfield | 994 Hilliard Davidson |
| 11 89 Sylvania Northview | 1186 Oak Hills |
| 12 87 Hilliard Bradley | 1280 Glenoak |
| 13 83 Olmsted Falls | 1369 Beavercreek |
| 14 76 Loveland | 1452 McKinley |
| 15 75 Athens | 1525 Lincoln |

Seven problems selected from the 40 that appeared on the 2016 tournament are shown in Figure 1. All of the problems can be solved using principles of algebra, geometry, and
arithmetic intermixed with strong problem solving skills. Calculators are always allowed on the OCTM tournament. Visit the contest website (www. octmtournament. org) for copies of previous contests as well as answers. Problems from these contests can be used with mathematics clubs or in math class to prepare mathletes for competition in 2017.

| 1. The points $(-2,0),(1,6)$, and $(a, 4)$ lie on the same line. Find the value of a. | $\begin{gathered} \text { ANSWERS } \\ -1 / 5 \end{gathered}$ |
| :---: | :---: |
| 2. If $\sqrt{x}=2(\sqrt[3]{y})=$, then find $x^{3}$ in terms of y | $64 y^{2}$ |
| 3. The graph of $y=a x^{2}+b x+c$ passes through $(2,0),(1,6)$ and $(0,8)$. Find the value of the product abc. | 0 |
| 4. What is the maximum value of $\sin ^{6} x+3 \sin ^{4} x \cos ^{2} x+3 \sin ^{2} x \cos ^{4} x+\cos ^{6} x$ | 1 |
| 5. In the figure shown, find a simplified expression for the shaded area. | $80 x(5 x-4)$ |
| 6. In the arithmetic series $20+16+12+\ldots$, what is the fewest number of terms (including the three given) needed so the sum is less than $\mathbf{- 2 0 1 6}$ ? | 38 |
| 7. Write the dimensions of a rectangle with integer side lengths that has the same perimeter as a 20 by 16 rectangle but with greater area. | 18 by 18 |

Fig. 1: A sampling from the 40 problems that appeared on the 2016 tournament test.

## 2 Preparations

Start assembling a team to represent your school in the 2017 tournament today. The 2017 tournament will take place on March 4, 2017 at test centers located throughout Ohio. Visit the tournament website to find a wealth of information about the State Tournament of Mathematics (www.octmtournament.org). One of the most important things we as teachers can do for our students is to make competition available. Competition helps build comradery, a lifelong interest in mathematics and a desire to achieve while building self-esteem to succeed. The calendar of events for the 2017 tournament is shown below. Hope to see your school as a participant in February at the 2017 State Tournament of Mathematics!

## 3 Contest Timeline of Events

September 15, 2016 Coaches Begin Sign-up
September 15, 2016
October 1, 2016
February 15, 2017
Student Tournament Registration Opens Online
Tournament Announcement Letter Mailed
Deadline for receiving Registration Fee without late fee. (no late fee if postmarked by this date)
February 22, 2017 LAST Day for receiving Registration Fee - must include $\$ 25.00$ late fee
February 22, 2017 Student Tournament Registration Closes - No Registrations accepted after this date.
February 27, 2017 Deadline for Coaches to Finalize Student List Online
March 4, 2017 Tournament Test Day held at 25 Ohio Sites


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